

3-4 and 3-5 Learn Check

In this Learning Check, you are being assessed on the following learning goals:
I can manipulate rational expressions into useful equivalent forms by simplifying, adding, subtracting, multiplying, and dividing.

Perform the following operations on the given rational expressions.

$$1. \frac{(x+2)^2}{x-3} \cdot \frac{x-3}{x^2+3x+2}$$

$$= \frac{\cancel{(x+2)}(x+2)}{\cancel{x-3}} \cdot \frac{\cancel{x-3}}{(x+2)(x+1)}$$

$$= \boxed{\frac{x+2}{x+1}}$$

$$2. \frac{2}{x^2+4x+3} + \frac{x}{x+1} \cdot \frac{(x+3)}{(x+3)}$$

$$(x+3)(x+1)$$

$$= \frac{2}{(x+3)(x+1)} + \frac{x^2+3x}{(x+3)(x+1)}$$

$$= \frac{x^2+3x+2}{(x+3)(x+1)}$$

$$= \frac{(x+2)\cancel{(x+1)}}{(x+3)\cancel{(x+1)}} = \boxed{\frac{x+2}{x+3}}$$

$$3. \frac{3-2x}{2x^2+5x-12} \cdot \frac{2}{x+4} \cdot \frac{2x-3}{2x-3}$$

$$(2x-3)(x+4)$$

$$= \frac{3-2x}{(2x-3)(x+4)} - \frac{(4x-6)}{(2x-3)(x+4)}$$

$$= \frac{9-6x}{(2x-3)(x+4)}$$

$$= \frac{3(3-2x)}{(2x-3)(x+4)} = \frac{-3(-3+2x)}{(2x-3)(x+4)} = \frac{-3\cancel{(2x-3)}}{\cancel{(2x-3)}(x+4)} = \boxed{\frac{-3}{x+4}}$$

$$4. \frac{x^2+4x+4}{x+3} \div \frac{6x+12}{3x^2+15x+18}$$

$$\frac{(x+2)(x+2)}{\cancel{x+3}} \cdot \frac{3\cancel{(x+2)}(x+3)}{6(x+2)}$$

$$= \boxed{\frac{(x+2)^2}{2}}$$

$$5. \frac{(x+2)x}{(x+2)(x-2)} - \frac{x^2+4}{x^2-4} + \frac{2}{x+2} \cdot \frac{(x-2)}{(x-2)}$$

$$= \frac{x^2+2x}{(x+2)(x-2)} - \frac{(x^2+4)}{(x+2)(x-2)} + \frac{2x-4}{(x+2)(x-2)}$$

$$= \frac{4x-8}{(x+2)(x-2)}$$

$$= \frac{4(x-2)}{(x+2)(x-2)}$$

$$= \boxed{\frac{4}{x+2}}$$